

Association Rules Mining Approach to Mineral Processing Control

Seraphin C. Abou and Thien-My Dao

Abstract — Mineral processes are multi-variable and power-intensive, strongly coupled with large delay and nonlinearities. The properties of controllability, observability and theory of minimal realization for linear systems are well understood and have been very useful in analyzing such systems. This paper deals with analogous questions for nonlinear systems with application to mineral processing. In many practical situations, standard asymptotic theory provides poor approximations, such as when the number of parameters is large or when the parameters are weakly identified. In this paper, a method that can control and provide accurate prediction of optimum milling condition and power consumption, water and chemical additive requirement is developed for mineral plants operation. A fuzzy mining algorithm is proposed for extracting implicit generalized knowledge on grading process performance as qualitative values. It integrates fuzzy-set concepts and generalized data mining technologies to achieve this purpose. Using a generalized similarity transformation for the error dynamics, simulation results show that under boundedness conditions the proposed approach guarantees the global exponential convergence of the error estimation. Although the nominal performance of the process is improved, the robust stability still is not guaranteed to fully avoid the mill plugging.

Index Terms— Association Rules Mining, Ball Mill, Fuzzy Logic, Nonlinear systems, Process control.

I. INTRODUCTION

Fuzzy control is a practical alternative for a variety of challenging control applications since it provides convenient methods for constructing nonlinear controllers via the use of heuristic information. A control-engineering method for fuzzy control is provided in [1].

Manuscript received July 26, 2009.

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We were concerned with both the construction of nonlinear controllers for challenging real-world applications and with gaining a fundamental understanding of the dynamics of fuzzy control systems so that we can mathematically verify their properties (e.g., stability) before implementation.

As a result, comprehensive solutions may be derived based on standard control theory and Lyapunov equations coupled with transcendental equations which characterize the variance of the signal at the saturation input. In mineral processing, understanding how to modify the rheological characteristics of fine particle systems is a key for the process performance. These characteristics include particle settling, pH, bulk/carrier fluid viscosity, particulate flocculation or dispersion, attrition, pipe/fitting/impeller wear, degradation of flocculated or friable solids and the pumpability of the slurry. Moreover, fine particle systems exhibit a range of rheological properties that influence processing and handling. The rheology of these systems is determined by both the physical properties and surface chemistry of the particles.

A wet grinding plant shown in fig.1 has been analyzed with the objective of evaluating the effects of many variables on particle size reduction in continuous grinding processes. Detailed phenomenological model that describes the charge behaviour has been developed and validated against real data [2]. Indeed, mineral processes present non-linear/chaotic dynamic behaviour. Considerable efforts have been developed in controlling such systems, [9], [10]. In [2], a comprehensive model integrating physical mechanisms and fundamental understanding of the charge behaviour was developed.

The grinding circuit consists of three variable velocity feeders, a main fixed velocity feeder, a ball mill, a sump, a variable velocity pump and a battery of hydro-cyclones. The fresh ore is transported towards the main feeder by the variable velocity feeders. Then it continues to the mill where water and the recirculated pulp are added. The output of the mill is stored in the sump and mixed with water, then, it is pumped to the battery of hydro-cyclones for classification. The fine

mineral pulp goes on to the flotation stage and the coarse mineral pulp is returned to the mill.

The literature review reveals that, the important factor of the poor quality of fine grinding (final product) is due to lacks of an appropriate control of the power draw of the mill. This causes increase of energy consumption, and production cost [4].

A classical PID controller is worthless to efficiently monitor the mineral plant. Through the past few decays, advanced control methods are being developed to address the system as a whole, dealing with all the problems that arise out of the complexity of the breakage process, its distributed nature, the networked interactions of the components, [5], [11]-[13]. Nevertheless, several approaches mainly depend on the model of the controlled plant. Although the mathematical model of the ball mill is advanced, it still remains so complex to fit very well for any Ball Mill design configurations.

In many applications of pattern classification which does not rely on the model of controlled plant, collecting enough labeled samples can be costly and time-consuming, whereas unlabeled ones are far easier to obtain. Training algorithm of neural network method makes it difficult to design a cost effective controller. However, Fuzzy control does not need the model of the controlled plant. Despite fuzzy control is an effective tool in complex processes monitoring, deriving Fuzzy logic rules is difficult.

In general, the fuzzy logic rules are obtained from the knowledge of experts and operators. As a result, the rules are limited, subjective and inaccurate. Although, in recent years, several fuzzy rules generation algorithms are discussed in [8], [9], [14], the algorithms have two mainly drawbacks: firstly, the algorithms need the training data which are not easily accessible; secondly some parameters and thresholds must be set beforehand, namely, different setting would generate different results.

Since its introduction in 1993, [3], the task association rule mining has received a great deal of attention. Association rules mining, which is one of core data mining tasks, finds interesting relationships among a large set of data items [10]. The association rules mining algorithm can be used on the service data directly and the uncovered relationships can be represented in the form of association rules. As a result, the mining results are not restricted to dependency analysis and could be directly adopted for the fuzzy logic controller as a control law.

II. GRINDING PROCESS MODELLING

Besides in *batch mode operation*, grinding circuit can operate in *continuous or fed-batch mode*. As shown in

fig.1, the motor load is strongly influenced by the filling percentage, the speed, the mill geometry and other relevant material properties such as stiffness and the coefficient of friction, etc...

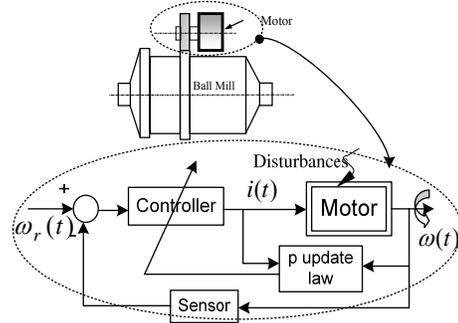


Fig.1. Motor servo-system of the Ball mill

The theoretical position of the charge at different rotation speeds was first derived by Davis, [4] based on the total force balance. In [4], a first order model is used to describe the breakage system. However, its use for practical solutions has a lack of its dependence on the physical parameters and grinding conditions. We are interested in the constitutive characteristics of the charge motion defined by a function $f(x, u)$ that better describes continuous grinding phenomena. From a macroscopic standpoint, the internal breakage model can be formulated taking in account the specifics phenomena of particle transport and size reductions:

$$\frac{\partial}{\partial t} [x(\cdot)] = \frac{\partial}{\partial z} \left[\Psi_n(\cdot) \frac{\partial m_i}{\partial z} - \Psi_n(\cdot) m_i \right] \quad (1)$$

where, m_i [kg], is particle mass of size i

The left side term of equation (1) expresses the rate of mineral production, while the term at the right side indicates fine particle transport phenomena. In this process with distributed parameters, function $\Psi_n(\cdot)$ that characterizes the particle size reduction, depends on many variables which are absolutely linked to system performance reliability. Therefore, without lacking for the physical sense for the process, we can write:

$$\Psi_n(\cdot) = \Psi_n(x, u) \quad (2)$$

Thus, we note the variation of the volume \mathbf{V} of the load of the Ball mill is important to the breakage mechanism efficiency as much as it is to the transport phenomena (i.e., breakage and the pulp transportation), but from a volumetric point of view both phenomena could be treated in a different way. Therefore, the fraction of the total mass broken within a tiny volume of the charge is assumed to be $\sigma(t)$ that is determined as follows:

$$\sigma(t) = \iiint_{\mathbf{V}} a \rho_c dV \quad (3)$$

where ρ_c is the charge bulk density, a is defined as a mass volume of material of classes i

Therefore, the flow rate of particle through the mill is:

$$\frac{d\sigma}{dt} = \iiint_V \frac{\partial(a\rho_c)}{\partial t} dV + \iiint_V a\rho_c \frac{d(dV)}{dt} \quad (4)$$

In addition, due to the absolute motion of the particle, the flux of the pulp could be used to define the flux associate to the fluid flow. However, as the mass could not be transferred by conduction phenomena, the mass flux therefore, vanishes, so that we could write:

$$\frac{d\sigma}{dt} = -\iint_F \vec{J}_i \cdot d\vec{F} + \iiint_V \mathcal{G}\sigma_p dV \quad (5)$$

where, \vec{J}_i :longitudinal diffusion flux of the mass in class i \mathcal{G} :piecewise parameter; σ_p : local fine particle.

The standard instrumentation in a grinding section includes the following sensors: volumetric flow sensor of the pulp flow towards the hydro-cyclones, pulp level sensor in the sump, power sensor in the mill, weight sensor in the feeder, sensor of water flow to the mill, sensor of water flow to the sump, pump velocity sensor, density sensor of pulp flow towards the hydro-cyclones, pump power sensor, etc. A systematic methodology, well-founded algorithms and related tools for design of controllers will have great impact in making advanced control of strategic importance to mineral processing.

III. THE CONTROLLER DESIGN

Wet comminution (grinding) and particle size classification can be effected by viscosity, particle size distribution, fines concentration etc. For example, hydrocyclone classification is effected by the presence of a yield stress (the minimum force required for slurry to flow). Often, cut point increases and efficiency decreases with increasing yield stress. The effects of these challenges can be further altered by process or environmental variables such as temperature or solids loading. The implementation of the mineral processing controller can be designed so that the process quality requirements are taken into account. This interlaced approach, called platform-based control design, can be developed using fuzzy logic controller based on association rules mining, [3].

The association rules mining algorithm uses the antecedent ergodicity and the single consequent link methods. The main problem of the grinding process lay in developing a sufficiently simple and reliable method for measuring the load in the Ball mill during operation. Although the fineness distribution capability of the particle can not be measured directly, it obviously is related to ball mill load, the stability of the grinding and the floatation processes. The ball mill load is referred to the ratio between the volume of raw material in the mill and the interstitial volume of the static ball charge. In

order to evaluate the behavior of the grinding process, the characteristics of its elements should be recognized firstly.

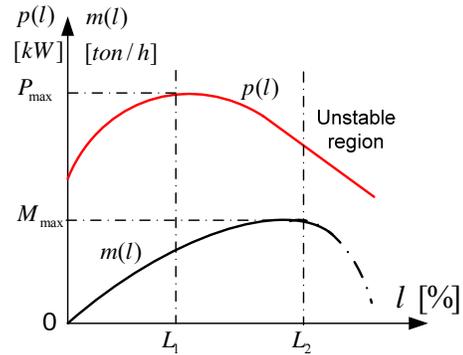


Fig.2. Static characteristics of Ball mill

Fig.2 depicts the characteristics of ball mill in function of the ball mill load, l . Functions $m(l)$ and $p(l)$ represent the grinding capability and the driving motor power, respectively. With the increase of the grinding capability, the outlet temperature and the inlet negative pressure must be controlled in certain ranges. Deviations from the established load lead to a sharp decrease of mill output and deterioration of the quality of grinding.

Our motivation is to design a fuzzy system to produce alarms and reconfigure the control variables if critical conditions occur in the process (pH, rheology, impeller wear, degradation of flocculated solids, slurry pumpability, etc.). Assume the fuzzy system uses $x_1(t)$, and $x_2(t)$ as inputs, and its output is an indication of what type of warning condition occurred along with the certainty that this warning condition has occurred. The alarm signals represent certain warnings characterized by the decision regions shown in Figure 3. For instance the density of the slurry is greater than the upper threshold limit; this occurs if: $x_1(t) > \alpha_1$ and $x_1(t) \geq x_2(t) + \alpha_3$

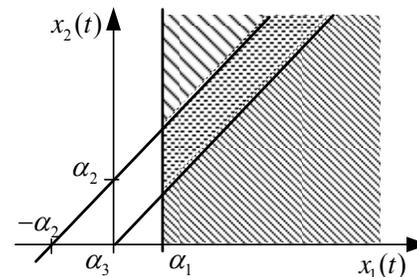


Fig.3 Decision regions for the rheology state

Small changes in chemical properties (in terms of lapping) may have large effects on the mineral quality and the grinding system dynamics. Especially, changes in the mill power draw parameters, which usually

provide the motion of the load of the mill, may result in the steady state error because of the dead-zone characteristics of the charge motion. In the next section, we consider the system as multi-state system.

Another important advance of fuzzy controller is a short rise time and a small overshoot with better performance than that of a standard PID controller. The grinding process is complex ill-defined process consisting of n elements, any element j , $1 \leq j \leq n$ can have k_j different states with corresponding performance rates (levels), which can be represented by the ordering set as follows, [9]:

$$g_j = \{g_{j1}, \dots, g_{ji_j}, \dots, g_{jk_j}\} \quad (6)$$

where g_{ji_j} is the performance rate (level) of the element j in the state i_j ; $i_j \in \{1, 2, \dots, k_j\}$.

The performance rate $G_j(t)$ of element j at any instant $t \geq 0$ is a random variable that takes its values from g_j : $G_j(t) \in g_j$. Thus, the probabilities associated with different states for the element j can be represented by a set: $p_j = \{p_{j1} \dots p_{ji_j} \dots, p_{jk_j}\}$

The mapping $g_{ji_j} \rightarrow p_{ji_j}$ is usually called the probability mass function as defined for multi-state system, [9]. There are two fundamental assumptions in the conventional multi-state system reliability theory: *i.*) each state probability of an element, which composed a multi-state system, can be fully characterized by probability measures; and *ii.*) the state performance rate (level) of an element, which composed a multi-state system, can be precisely determined. However for some multi-state systems, evaluating precisely the state probability and performance rate of an element is difficult. Some reasons come from inaccuracy and insufficiency of data.

As above pointed out for the cause of the deterioration of the grinding quality, let define the error e_r and change of error e_c at sampled times k as follows:

$$\begin{cases} e_r(k) = \frac{p(k) - p(k-1)}{V_m(k) - V_m(k-1)} \\ e_c(k) = e_r(k) - e_r(k-1) \end{cases} \quad (7)$$

The variable p can be measured by means of measuring the electric current of the ball mill. At each moment, the system elements have certain performance levels corresponding to their states. Due to the complexity of the grinding system, its state is determined by the states of its elements. The

performance rates of the system are determined by the performance levels of its elements. As a result, the independence of the evidence to be combined would obviously be satisfied if all models were completely different, that is, had no overlapping equations. A conventional controller design procedure does not guarantee this and it may not even be possible to design such a set of models.

Note that the overlapping equations exist in a different environment in each model. This is sufficient for the independence of evidence, in the sense that noise and modeling errors will cause different distortions to the probability assignments in the different models.

Assume the probability distribution σ_d of performance rates for all of the system elements at any instant $t \geq 0$ and system structure function as follows:

$$\begin{cases} g_j, p_j \rightarrow 1 \leq j \leq n \\ \phi(G_1(t) \dots G_n) \end{cases} \quad (8)$$

Accordingly, the total number of possible states or performance rates of the system is:

$$\pi_p = \prod_{j=1}^n k_j \quad (9)$$

Let $L^n = \{g_{11}, \dots, g_{1k_1}\} \times \dots \times \{g_{j1}, \dots, g_{jk_j}\} \times \dots \times \{g_{n1}, \dots, g_{nk_n}\}$ be the space of possible combinations of performance rates for all system elements and $M = \{g_1, \dots, g_{\pi_p}\}$ be the space of possible values of entire system performance levels.

The transform $\phi(G_1(t) \dots G_n(t)): L^n \rightarrow M$ which maps the space of performance rates of system elements into the space of system's performance rates, is the system structure function, [14].

The probability of the system state is given as:

$$\sigma_i = \prod_{j=1}^n \sigma_{ji_j}; \text{ the performance rate for state } i \text{ is:}$$

$$g_i = \phi(g_{ni_1}, \dots, g_{ni_n}) \quad (10)$$

For the system under consideration, the estimation of a single number for the probabilities and performance levels is very difficult. Other reasons come from the model simplification. Each system element may have many different states and sometimes it may even have continuous performance. To avoid the "dimension damnation", the model is reduced to decrease the computational burden.

Fuzzy logic controllers (FLC) have the advantage to be robust and relatively simple to design since they do not require the knowledge of the exact model. However,

we need complete knowledge of the system operation. The fuzzy system that serves the implementation of general decision-making in tuning the driving motor power of the mill is presented in Fig.4.

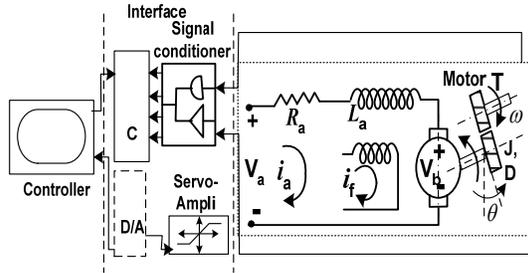


Fig.4 Hardware setup

We proposed in this study fuzzy logic controller with discrete inverses based on association rules mining. It has three inputs and outputs. The tuned control surface is nonlinearity corresponding to the property of controlled plant. l , ω_r and n_p are the measured value of the ball mill load, the rotation speed and the inlet negative pressure, respectively. In addition, p is the measured value of the ball mill driving motor power. e_l , e_ω and e_{np} which are input variables of the fuzzy logic controller, represent the error of l , ω_r and n_p respectively. u_l , u_ω and u_{np} are the output variables of the fuzzy logic controller, which are usually used to control the raw ore feeder, the driving motor speed and the recycle air damper, respectively.

Therefore, the probability distribution σ_d of the system is:
$$\phi(g_{1i_1}, \dots, g_{3i_3}), \sigma_d = \prod_{j=1}^3 \sigma_{ji_j} \quad (11)$$

Furthermore, the max-min algorithm is used in fuzzy logic inference, and the defuzzification is accomplished by the largest of maximum method.

A. Fuzzy Logic Controller

In the fuzzy control design methodology, we made use of heuristic information as from an operator who has acted as a “human-in-the-loop” controller for the process. To develop a set of rules applicable to mineral processing control, the practical expertise is drawn on our knowledge performed through extensive mathematical modeling, analysis, and development of control algorithms for diverse processes. Then we incorporate these into a fuzzy controller that emulates the decision-making process of the human, Fig.5.

The function $\phi(\cdot)$, (11) is strictly defined by the type of connection between elements in the reliability logic-diagram sense, i.e. on the structure of the logic-diagram representing the system/subsystem.

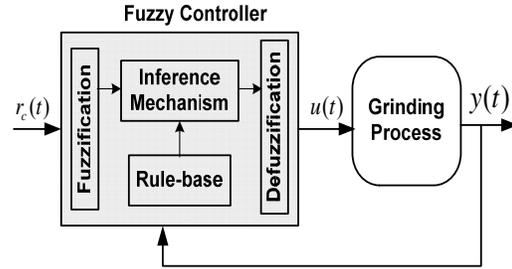


Fig.5 Fuzzy controller architecture

Despite the fact that the universal generating function resembles a polynomial, it is not a polynomial because: *i.*) its exponents are not necessary scalar variables, but can be arbitrary mathematical objects (e.g. vectors); *ii.*) operators defined over the universal generating function can differ from the operator of the polynomial product (unlike the ordinary generating function technique, only the product of polynomials is defined) [6].

Fig.6 idealizes a general flow transmission through out the system (e.g., ore, particle size, fluid flow, energy). For instance, consider a flow transmission system shown in fig.6 which consists of three elements. As a result, the system performance rate which is defined by its transmission capacity can have several discrete values depending on the state of control equipments.

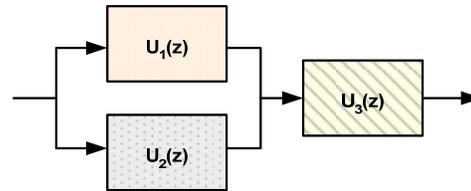


Fig.6. A flow transmission structure

Assume the element 1, (the slurry rheology) has three states with the performance rates: $g_{11} = 1.5$, $g_{12} = 1$, and $g_{13} = 0$; the corresponding probabilities are respectively: $\sigma_{p11} = 0.8$, $\sigma_{p12} = 0.1$ and $\sigma_{p13} = 0.1$. The element 2, (the pH) has three states with the performance rates $g_{21} = 2$, $g_{22} = 1.5$, $g_{23} = 0$ and the corresponding probabilities $\sigma_{p21} = 0.7$, $\sigma_{p22} = 0.22$ and $\sigma_{p23} = 0.08$. The element 3, (the density) has two states with the performance rates $g_{31} = 4$, $g_{32} = 0$ and the corresponding probabilities $\sigma_{p31} = 0.98$ and $\sigma_{p32} = 0.02$. According to (9) the total number of possible combinations of the states of elements is $\pi_p = 3 \times 3 \times 2 = 18$.

In order to obtain the output σ_p for entire system with the arbitrary structure function $\phi(\cdot)$, [8] used a general composition operator $\hat{\partial}_\phi$ over individual

universal z -transform representations of n system elements:

$$\begin{cases} U(z) = \partial_\phi(u_1(z), \dots, u_n(z)) \\ u(z) = \sum_{i=1}^{k_j} \sigma_{dji} \cdot z^{g_{ji}} \end{cases} \quad (12)$$

$$U(z) = \sum_{i_1}^{k_1} \sum_{i_2}^{k_2} \dots \sum_{i_n}^{k_n} \left(\prod_{j=1}^n \sigma_{dji} \cdot z^{\phi(g_{ji}, \dots, g_{ni_n})} \right)$$

where $U(z)$ is z -transform representation of output performance distribution for the entire system.

Figure 5 illustrates the basic control structure. The scheme includes a classical PID control structure together with fuzzy corrector. The fuzzy corrector uses the command input $r_c(t)$ and the plant output y to generate a command signal $u_c(t)$, described by the following equations:

$$\begin{cases} e(t) = r_c(t) - y(t) \\ \Delta e(k) = e(k) - e(k-1) \\ \mu(k) = F[e(k), \Delta e(k)] \end{cases} \quad (13)$$

In the above, $e(k)$ is the position error between the command input $r_c(t)$ and the process output $y(k)$; $\Delta e(k)$ is the change in position error. The term $F[e(k), \Delta e(k)]$ is a nonlinear mapping of $e(k)$ and $\Delta e(k)$ based on fuzzy logic. The term $\mu(k)$ represents a correction term. The control $u(k)$ is applied to the input of the grinding circuit. The purpose of the fuzzy corrector is to modify the command signal to compensate for the overshoots and undershoots present in the output response when the load dynamics has unknown nonlinearities.

Consider x_1, x_2, x_3, y_1, y_2 and y_3 represent $l, \omega_r, n_p, u_l, u_\omega$ and u_{np} respectively. The expertise and knowledge method used to build a rule base and membership functions provide the description of $e(k)$ and $\Delta e(k)$ as inputs, and $\mu(k)$ as the output.

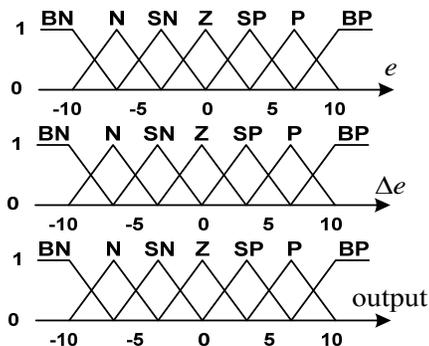


Fig.7 The Fuzzy sets

The unified fuzzy inverse is given as $[-0.1, 0.1]$, fig.8. The fuzzy states of the inputs and the output, all are chosen to be equal in number and use the same linguistic descriptors: *Big Negative* (BN), *Negative* (N), *Small Negative* (SN), *Zero* (Z), *Small Positive* (SP), *Positive* (P) and *Big Positive* (BP). Fig.8 illustrates the membership functions.

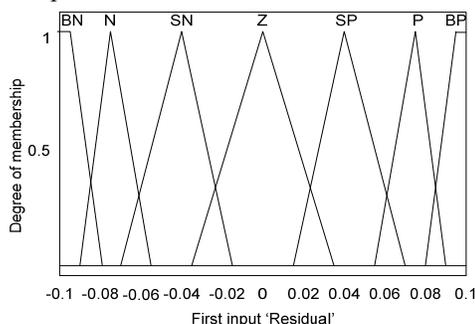


Fig. 8 Membership functions

Despite the operator expertise and knowledge at the level of the inference rules and the membership functions, some defects may appear. The degree of membership of each value of attribute i_k in any of its fuzzy sets is directly based on the evaluation of the membership function of the particular fuzzy set with the value of i_k as input. To improve the conventional FLC, association rules mining algorithms are used to find the optimal membership functions. This is achieved according to the following stages.

B. Association rules Mining Algorithm

Specified fuzzy linguistic terms in fuzzy association rules can be given only when the properties of the attributes are estimated. In real life, contents of columns (i.e., values of attributes) may be unknown and meaningful intervals are usually not concise and crisp enough. In this paper, the target is to find out some interesting and potentially useful regularities, i.e., fuzzy association rules with enough support and high confidence. We use the following form for fuzzy association rules.

Let be $\{x_i^1, \dots, x_i^k\}$ and $\{y_i^1, \dots, y_i^k\}$ the antecedent set and the consequence set respectively, in a database. A fuzzy association rule mining is expressed as:

$$\text{If } X = \{x_i^1, \dots, x_i^k\} \text{ is } A = \{\alpha_i^1, \dots, \alpha_i^k\} \rightarrow \text{Then } Y = \{y_i^1, \dots, y_i^k\} \text{ is } B = \{\delta_i^1, \dots, \delta_i^k\}$$

Here, X and Y are disjoint sets of attributes called item-sets, i.e., $X \subset I; Y \subset I$ and $X \cap Y = \emptyset$. A and B contain the fuzzy sets associated with corresponding attributes in X and Y , respectively.

Let $\mu(\cdot)$ represent the membership value of each element of the antecedent and the consequence set. Under fuzzy taxonomies, using the measurements could result in some mistakes. Consider for instance the following conditions:

$$1- \mu(x_i^k) \geq \mu(y_i^k) \text{ and } \mu(x_i^k) \geq \mu(y_i^m)$$

$$2- \mu(x_i^k) < \mu(y_i^k) \text{ and } \mu(x_i^k) < \mu(y_i^m)$$

In the first condition, the confidence under fuzzy taxonomies of the two rules is equal, while in the second, the coverage of the two rules is equal. This situation rise the following question: *which rule can be judged as best evidence rule?*

For a rule to be interesting, it should have enough support and high confidence value, larger than user specified thresholds. To generate fuzzy association rules, all sets of items that have a support above a user specified threshold should be determined first. Item-sets with at least a minimum support are called frequent or large item-sets.

In the proposed method the algorithm iterations alternate between the generation of the candidate and frequent item-sets until large item-sets are identified. The fuzzy support value of item-set Z is calculated as:

$$S(Z, F) = \frac{\sum_{t_i \in T} \prod_{z_j \in Z} \mu(\alpha_j \in F, t_i(z_j))}{n_T} \quad (14)$$

where n_T is the number of transactions in the database.

Also, to ensure the accuracy of rules base, the consequent strength measure, ψ is used to estimate the mined rules as:

$$\psi = \sum_{i=1}^n \left(\prod_{k=1}^{k_x} \mu(y_i^k) \wedge \prod_{m=1}^{k_y} \mu(y_i^m) \right) \cdot \sum_{i=1}^n \prod_{j=1}^{k_y} \mu(y_i^j) \quad (15)$$

Based on the literature review, the fuzzy-PID control is implemented in such way that the fuzzy system has $\dot{\psi}$ (derivative of the PID output) as input and returns an output \dot{g} that has a nonlinear dependence upon the input. The dependence upon $\dot{\psi}$ ensures that changes in the steady value of ψ do not change the closed-loop response characteristics of the fuzzy-PID controller. Hence the simplest form of fuzzy-PID controller is:

$$\frac{dg}{d\tau} = \frac{1}{\beta} f \left(\alpha \frac{d\psi}{d\tau} \right) \quad (16)$$

where α is an input scaling factor and β is an output scaling factor. The input magnitude is scaled to unity by:

$$\alpha = \left(\max \left(\left| \frac{d\psi}{d\tau} \right| \right) \right)^{-1} \quad (17)$$

The evaluation of $\max \left(\left| \frac{d\psi}{d\tau} \right| \right)$ is normally estimated from one or more PID runs. The final system implemented is presented as:

$$f(\zeta) = \begin{cases} \varphi \zeta (|\zeta|(\varphi-1) + 1)^{-1} & \text{for } |\zeta| \leq 1 \\ -1 & \text{for } \zeta \leq -1 \\ 1 & \text{for } \zeta \geq 1 \end{cases} \quad (18)$$

The graph of the function $f(\zeta)$ is presented in figure 9. It depicts sigmoidal dependence on ζ . As a result, it may corrupt all slowly varying signals of the process.

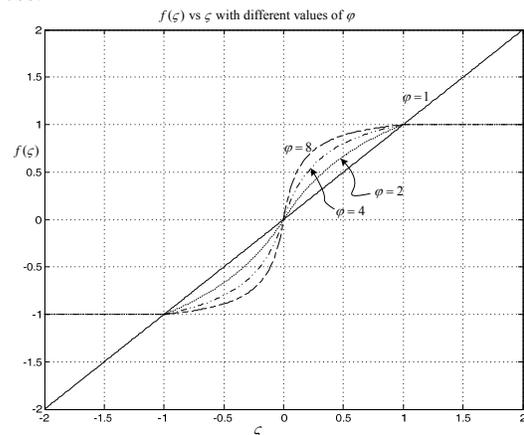


Fig.9 $f(\zeta)$ with varying φ

In order to suppress the noise and get the nonlinear control surface, the parameters of input membership functions and output membership functions of the fuzzy rule base is tuned by a nonlinear optimization. In this study a sequential quadratic programming (SQP) algorithm as presented in Matlab is used. This approach represents state-of-the-art in non-linear programming methods, because a non-linearly constrained problem can often be solved in fewer iterations using SQP than an unconstrained problem. One of the reasons is that due to the limits on the feasible area, the optimizer can make well informed decisions regarding directions of search and step length.

Note that widely overlapping membership functions give good numerical results. However, fuzzy membership functions lacking any physical interpretation and loosing locality are possible. To avoid this, different kinds of constraints may be put on the optimization: kinds of constraints, inequality constraints and parameter bounds. SQP efficiently solve this

constrained nonlinear optimization problem in which the objective function and constraints may be nonlinear functions of variables.

IV. SIMULATION RESULTS

Through available actuators it is possible to adjust the speed of the grinding circuit feeders, the fluid added to the mill and sump, the pump and the driving motor speed. The level of the sump is controlled by adjusting the set-point of pump velocity.

The water flow to the flotation circuit is kept proportional to the load reference. As mentioned, the above process is subject to many disturbances, being the hardness of the raw feeding ore the most significant one. This exerts a strong influence on the quality of the grinding product. Modeling of the process is further complicated by the fact that different operation points are defined by changes in mineral hardness.

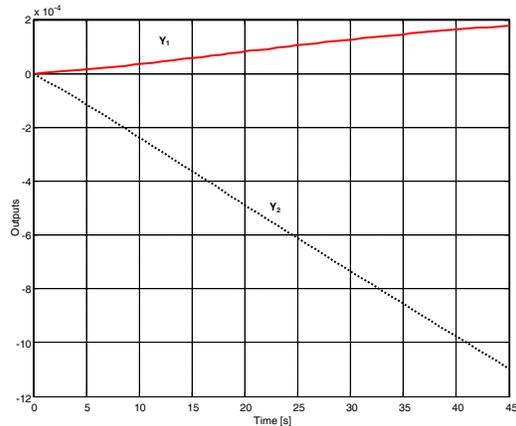


Fig.10 Coupling degree of breakage process

Based on a reasonably simple transfer function, the adjustable input ports of the driving motor and entrance negative pressure of the breakage circuit are initialized with step signal. Fig.10 illustrates coupling phenomena that exists between the controller variables (e.g., the entrance of negative pressure and the motor rotation speed).

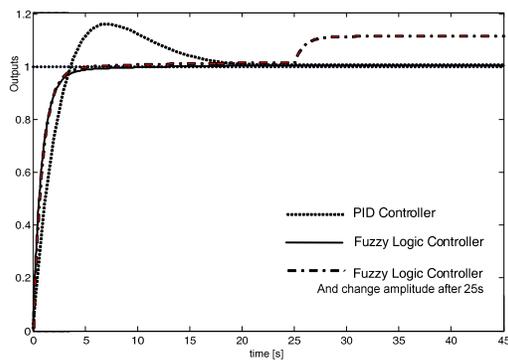


Fig. 11 Fuzzy Logic Controller step response

Using the aforementioned fuzzy logic rules the simulated step response of the grinding circuit is shown in fig.11.

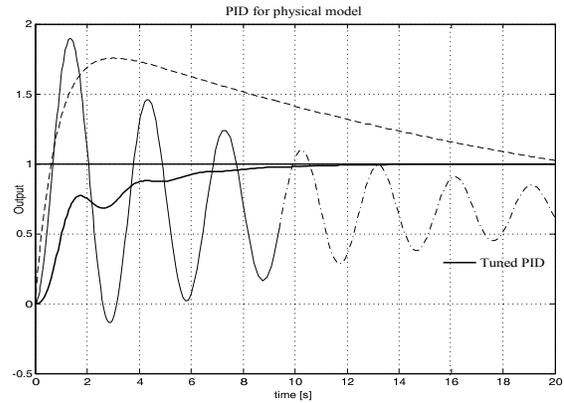


Fig. 12 Tuned PID

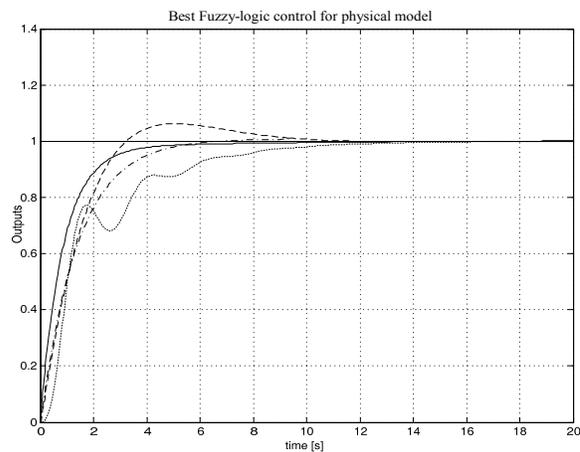


Fig.13 Tuned fuzzy logic Controller using physical model

As shown in fig.13, in the presence of disturbances the fuzzy logic controller model presents a response better than the conventional PID model.

V. CONCLUSION

In mineral processing, understanding how to modify the rheological characteristics of fine particle systems is a key for the process performance. Constrained optimization methods with integrated association rules mining based on a nonlinear, fuzzy dynamic control scheme were designed to improve the grinding process. The proposed structure of fuzzy logic controller combines the advantages of the fuzzy networks approach and the association mining rules. Indeed, due to its ability to approximate nonlinear function and its fast convergence, the proposed method is an approximation tool to generate a control signal. With the proposed algorithms the process can be controlled in a better way than the conventional PID approach, as it was demonstrated during the design of the control

algorithm. Simulation results show that the association rules mining algorithm is a feasible control rules generation algorithm to the fuzzy logic controller. Obviously, it can be deduced that the fuzzy controller is faster than the conventional controller in the transitional state, and also presents a much smoother signal with less fluctuations in steady state. The proposed method can overcome nonlinear and strong coupling features of mineral processing in a wide range. The proposed method has a strong adaptability.

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