# Reducing Peak Transmission Power of OFDM System Using Signal Partition Technique

Yingxin Zhao, Yue Wu and Hong Wu

Abstract—A new spread spectrum Orthogonal-Frequency-Division-Multiplexing (OFDM) system using a novel signal partition method is proposed. The time domain signals after Inversion-Fast-Fourier-Transform (IFFT) are divided into one continuous segment and several discrete segments and sent out after interleaving. At the receiving end, a unique demodulation method called partial signal restoration is further proposed. Simulation results show that the proposed system, with low computation complexity, can significantly increase the BER performance while the peak transmission power can be reduced obviously.

*Index Terms*—OFDM, PAPR, Spread spectrum, Signal partition

# I. INTRODUCTION

ne of the major drawbacks of Orthogonal-Frequency-Division-Multiplexing (OFDM) systems is that the OFDM signal exhibits high peak power [1-3]. When the peak power lies in the saturation region of the power amplifier, the output signal would suffer from nonlinear distortion, leading to spectrum spreading, in-band distortion and intermodulation interference across the OFDM subcarriers [4-6], which severely degrade the bit error rate (BER) performance at the receiving end. Great efforts have been made to reduce the peak power[7], such as partial transmit sequences (PTS) algorithm [8-11] and selected mapping (SLM) algorithm [12-14]. Saberian and Tewfik [15] proposed a spectrum-spreading based OFDM system by using a sigma-delta modulator for UWB communication, where the peak to average power ratio (PAPR) of this system equals one, while the spectral efficiency was also reduced as expense due to the quantization noise of the sigma-delta converter. In this paper, we propose a new spread spectrum OFDM system using a novel signal partition method,

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Hong Wu is with Key Laboratory of Photonics Materials and Technology for Information Science, College of Electronic Information and Optical Engineering, Nankai University, Tianjin, China(e-mail: wuhong@nankai.edu.cn). which we call mixed signal partition. The time domain signals after Inversion-Fast-Fourier- Transform (IFFT) are divided into one continuous segment and several discrete segments and sent out after interleaving. At the receiving end, we further propose a unique demodulation method, partial signal restoration, to demodulate the discrete segments. The restored discrete data, together with the continuous segment, are further deinterleaved and combined. Simulation results show that the proposed system improves the BER performance and reduces the peak transmission power with low computation complexity. This paper is organized as follows: The proposed OFDM system is introduced in Section II. The simulation results are presented and discussed in Section III. Section IV concludes this paper.

#### II. MIXED SIGNAL PARTITION TECHNIQUE

# A. Mixed Signal Partition of the Signals

The block diagram of the proposed system is show in Fig.1. Different from the conventional OFDM system, we add a signal partition and interleaving module after the IFFT process at the transmitter, and a deinterleaving and signal combination module at the receiver. For illustration, the signal partition and interleaving at the transmitter side would be first introduced.

Specifically, the real parts  $x_i$  and the imaginary parts  $y_i$  of the time domain signals from N point IFFT are separated and clipped so that the amplitude of each part of the signal is under a certain level *CL*, where the clipping level *CL* is determined by the BER degradation tolerance. After clipping,  $x_i$  and  $y_i$  are partitioned into K segments, where K is a positive integer. For illustration, let us take the real part, i.e.,  $x_i$  as an example. Denote  $x_{i1}, x_{i2}, ..., x_{iK}$  as the K segments divided from real part  $x_i$ , where i = 0, 1, ..., N-1. When K = 1, it is the same as the conventional OFDM.

When K = 2, the rules of partition can be written as:

$$\begin{aligned} x_{i1} &= a, & x_{i2} = CL - a. & \text{if } x_i > CL \\ x_{i1} &= a, & x_{i2} = x_i - a. & \text{if } a < x_i \le CL \\ x_{i1} &= 0, & x_{i2} = x_i. & \text{if } -a \le x_i \le a \\ x_{i1} &= -a, & x_{i2} = x_i + a. & \text{if } -CL \le x_i < -a \\ x_{i1} &= -a, & x_{i2} = a - CL. & \text{if } x_i < -CL \end{aligned}$$
(1)

where *a* is a positive real number,  $a \le CL/2$ .



Fig.1 Block diagram of the system

When  $K \ge 3$ , the rules of partition can be written as:  $x_{i1} = a, x_{i2} = a, \dots, x_{iK-1} = a, x_{ik} = CL - (K-1)a.$ if  $x_i > CL$  $x_{i1} = a, x_{i2} = a, \dots, x_{iK-1} = a, x_{iK} = x_i - (K-1)a.$ if  $(K-1)a < x_i \le CL$  $x_{i1} = a, \dots, x_{i_{n-1}} = a, x_{i_n} = 0, \dots, x_{i_{K-1}} = 0, x_{i_K} = x_i - (n-1)a.$ if  $(n-1)a < x_i \le na, n = 2, 3, \dots, K-1$  $x_{i1} = 0, \ x_{i2} = 0, \cdots, x_{iK-1} = 0, \ x_{iK} = x_i.$ (2) if  $-a < x_i \le a$  $x_{i1} = -a, \dots, x_{i_{n-1}} = -a, x_{i_n} = 0, \dots, x_{i_{K-1}} = 0, x_{i_K} = x_i + (n-1)a.$ if  $-na \le x_i \le -(n-1)a, n = 2, 3, \dots, K-1$  $x_{i1} = -a, x_{i2} = -a, \dots, x_{iK-1} = -a, x_{iK} = x_i + (K-1)a.$ if  $-CL < x_i \leq -(K-1)a$  $x_{i1} = -a, x_{i2} = -a, \dots, x_{iK-1} = -a, x_{iK} = (K-1)a - CL.$ if  $x_i < -CL$ 

The imaginary parts  $y_i$  can also be partitioned according to (1-2). The peak power of the partitioned signals is closely related to the selection of a. It is obvious that the peak power can be minimized when a = CL/K.

From (1) and (2), we can observe that the signals are partitioned into one segment with continuous values and K-1 segments with discrete values, which is known as mixed signal partition.

In fact, the partition here can be interpreted as quantization, where the discrete segments correspond to the quantum level and the continuous segment corresponds to the quantizing error.

#### B. Method of Interleaving

After the signal partition, we order the sequences of the partitioned signals as

$$x_{01}, x_{11}, \dots, x_{N-1,1}, x_{02}, x_{12}, \dots, x_{N-1,2}, \dots, x_K, x_{1K}, \dots, x_{N-1,K}$$
 in channel and

 $y_{01}, y_{11}, \dots, y_{N-1,1}, y_{02}, y_{12}, \dots, y_{N-1,2}, \dots, y_{0K}, y_{1K}, \dots, y_{N-1,K}$ 

in Q channel. This order is determined by the properties of Discrete Fourier Transform (DFT).

# C. Example

To illustrate our proposed method, we would like take the Quadrature Amplitude Modulation (QAM) signals as an example. Suppose that we have four QAM signal, 1-j, -1+j, -1-j, 1+j. After a 4 point IFFT, we get four time

domain data, 0, 
$$\frac{1}{2}(1+j)$$
,  $j$ ,  $\frac{1}{2}(1-j)$ .

Setting CL = 0.9, a = 0.225, we get following data:

$$\begin{aligned} x_0 &= \{0, 0, 0, 0\} & y_0 &= \{0, 0, 0, 0\} \\ x_1 &= \{a, a, 0, 0.05\} & y_1 &= \{a, a, 0, 0.05\} \\ x_2 &= \{0, 0, 0, 0\} & y_2 &= \{a, a, a, 0.225\} \\ x_3 &= \{a, a, 0, 0.05\} & y_3 &= \{-a, -a, 0, -0.05\} \end{aligned}$$

After interleaving, the I channel signal is:

and Q channel signal is :

 $\{0, a, a, -a, 0, a, a, -a, 0, 0, a, 0, 0, 0.05, 0.225, -0.05\}.$ 

#### D. Receiver Structure

According to the property of the signal, we propose a unique demodulation method, called partial signal restoration (PSR). The I/Q channel signals are separated after synchronization. The received signals corresponding to the discrete segments are estimated and detected, and finally restored to  $\hat{a}$ , 0 or  $-\hat{a}$ . Together with received continuous segment, the restored data are deinterleaved and combined. After FFT and data recovery, the original data can be obtained. Note that although the channel noise is removed from the received discrete segments, the performance may be degraded by the decision errors.

# E. Average Power, PAPR and Processing Gain

If f(x) is an even probability distribution function of  $x_i$  or  $y_i$ , the total average power of two segments partition will

be:  

$$P_{tot} = 4 \int_{0}^{a} x^{2} f(x) dx \qquad (3)$$

$$+4 \int_{a}^{CL} [(x-a)^{2} + a^{2}] f(x) dx + 4 \int_{CL}^{\infty} [(CL-a)^{2} + a^{2}] f(x) dx \qquad (4)$$
When  $K \ge 3$ ,  

$$P_{tot} = 4 \int_{0}^{a} x^{2} f(x) dx \qquad (4)$$

$$+4 \sum_{n=1}^{K-2} \int_{na}^{(n+1)a} [(x-na)^{2} + na^{2}] f(x) dx \qquad (4)$$

$$+4 \int_{(K-1)a}^{CL} \{ [(x-(K-1)a]^{2} + (K-1)a^{2}] f(x) dx \qquad (4)$$

Because the clipping is carried out at  $x_i$  or  $y_i$  individually, the average power is slightly less than that under ordinary clipping.

According to the Centre Limit Theorem, f(x) converges to the normal distribution when N is large.

$$f(x) = \frac{1}{\sqrt{2\pi\sigma}} e^{-\frac{x^2}{2\sigma^2}}$$
(5)

where  $\sigma$  is the standard deviation of  $x_i$  or  $y_i$ .

The processing gain of spread spectrum here could be written as:

Processing Gain

$$=10\log\frac{\text{the average power of the original signal}}{\text{the total average power of K parts}}$$
(6)

= 
$$10\log\frac{2\sigma^2}{P_{tot}}$$

The Peak to Average Power Ratio (PAPR) is mainly determined by the clipping level. Partition reduces not only peak power, but also average power. The value a should be properly selected to decrease the PAPR. The PAPR after partition is given by

$$PAPR = \frac{2[CL - (K - 1)a]^2}{P_{tot} / K}$$
(7)

For example, when N = 64,  $CL = 2\sigma$ ,  $a = \sigma$  and K = 2, calculated  $P_{tot}$  is 1.243 $\sigma^2$ , PAPR is 5.08dB and Processing Gain is 2.07dB.

## III. RESULTS OF COMPUTER SIMULATION

In our simulation, the input signals to IFFT are QPSK and 16QAM. At first, the *CL* levels were set by experiment. The levels are selected as  $2\sigma$  for QPSK input and  $2.6\sigma$  for 16QAM input, because the two clipping levels cause little BER degradation.

Fig.2 shows the simulation results of the BER performance of QPSK input with 2 segments partition. The curve labeled without PSR is also plotted for comparison. We can see from Fig. 2 that the BER curve without PSR is 2dB worse than our proposed method, which verified our analysis on the processing gain. By comparing the curve with PSR and the curve clipping,

we can see from Fig.2 that the SNR improvement is 3.65dB at  $10^{-4}$  BER. The PAPR resulted from clipping is 6.02dB and that after partition is 5.08dB. Therefore, a 4.59dB reduction of the transmitter peak power can be achieved.

Fig.3 is shows the BER performance of QPSK input with 4 segments partition. SNR improvement is 5.65dB. The PAPR after partition is 2.85dB. So the transmitter peak power is reduced by 8.82dB.



Fig.2 BER performance of QPSK-OFDM system with  $K = 2, a = \sigma, N = 64$ and  $CL = 2\sigma$  in AWGN channel



Fig.3 BER performance of QPSK-OFDM system with  $K = 4, a = 0.5\sigma, N = 64$  and  $CL = 2\sigma$  in AWGN channel

Fig.4 is the BER performance of 16QAM input with 2 segments partition. The SNR improvement is 4.2dB at  $10^{-4}$  BER. The PAPR of clipping is 8.30dB and that after partition is 7.48dB. So the reduction of the peak power is 5.02dB.

Fig.5 is the BER performance of 16QAM input with 4 segments partition. The calculated processing gain is 3.5dB. This is shown by the curve labeled without PSR. The calculated PAPR values are 8.30dB and 5.78dB for clipping and partition respectively. At  $10^{-4}$  BER, the SNR improvement is 9.35dB. So the peak transmission power is reduced by 11.87dB.

Table I summarizes the results of peak power reduction after partition. We can see the peak transmission power can be significantly reduced by our proposed method. The results with maximum 11.87dB reduction are very significant.

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Fig.5 BER performance of 16QAM-OFDM with  $K = 4, a = 0.65\sigma, N=32$ and  $CL = 2.6\sigma$  in AWGN channel

TABLE I				
TRANSMITTER PEAK POWER REDUCTION				
Combination	Peak power reduction(dB)			
QPSK, $K = 2$	4.59			
QPSK, $K = 4$	8.82			
16QAM, <i>K</i> = 2	5.02			
16QAM, $K = 4$	11.87			

The comparison of the three combinations with the same bandwidth is further plotted in Fig.6. 128 point BPSK input, 64 point QPSK input at K = 2, and 32 point 16QAM input at K = 4 are used in simulation. Table II lists the results. Comparing with BPSK input, we can see that the peak transmission power of QPSK input and K = 2 decreases 1.44dB at  $10^{-4}$  BER.

Fig.7 is a comparison of the BER performance with 64-tone sigma-delta method in AWGN channel. The interpolation factor *L* is 4 in 64-tone sigma-delta method. The parameters of the spread spectrum method are  $K = 4, a = 0.5\sigma, CL = 2\sigma$ . The original signal is N = 64, QPSK-OFDM and the bandwidth expansion of the two methods is the same. Table III lists the comparison results. We can see that at BER=10<sup>-2</sup>, the needed average power of 64-tone sigma delta is 6.8dB higher than the

proposed spread spectrum method. And although the PAPR of 64-tone sigma delta is 0dB, the peak power is still 1.54dB higher than the later.



Fig.6 Comparison of BER performance of BPSK with  $CL = 2\sigma$ , QPSK with  $CL = 2\sigma$ , K = 2,  $a = \sigma$ , 16QAM-OFDM with  $CL = 2.6\sigma$ , K = 4,  $a = 0.65\sigma$  in AWGN channel

TABLE II	
COMPARISON OF THE THREE COMBINATION	ONS

COMPARISON OF THE THREE COMBINATIONS							
Combination	Point number of IFFT and FFT	S/N(dB) at 10 <sup>-4</sup> BER	PAPR (dB)	Relative peak power (dB)			
BPSK, $CL = 2\sigma$	128	9.45	6.02	0			
QPSK, $CL = 2\sigma$ $K = 2, a = \sigma$	64	8.95	5.08	-1.44			
16QAM, $CL = 2.6\sigma$ $K = 4, a = 0.65\sigma$	32	10.65	5.78	0.96			



Fig.7 Comparison of BER performance of sigma-delta method with N = 64, L = 4 and spread spectrum method with  $N = 64, K = 4, a = 0.5\sigma, CL = 2\sigma$  in AWGN channel

TABLE III Comparison Results of the two methods						
Method	S/N(dB) at 10 <sup>-2</sup> BER	PAPR (dB)	Relative peak power(dB)			
64-tone Sigma-delta	10.7	0	0			
Mixed Signal Spread Spectrum	3.9	4.56	-1.54			

# IV. CONCLUSION

To reduce the peak transmission power of an OFDM system, a mixed signal partition technique is proposed. Simulation results verify that the proposed OFDM system can significantly improve the system performance. For instance, the mixed signal partition will increase S/N by an amount equal to processing gain. The BER performance is further reduced by the PSR method. The peak transmission power can be significantly reduced by our proposed method.

#### REFERENCES

- M. G. Sumithra, M. Sarumathi, "Comparative analysis of PAPR reduction techniques for multicarrier systems", 2012 International Conference on Computer Communication and Informatics, Vietnam, pp1-5, 2012
- [2] E. G. Lim, J. C. Wang, Z. Wang, T. Tillo, and K. L. Man, "The UHF Band In-body Antennas for Wireless Capsule Endoscopy", Engineering Letters, vol.21, no.2, pp72-80,2013
- [3] M. A. Salam, M. A. Rashid, Q. M. Rahman, and M. Rizon, "Transient Stability Analysis of a Three-machine Nine Bus Power System Network", Engineering Letters, vol.22, no.1, pp1-7,2014
- [4] Da Costa Pinto F, Scoralick F S O, De Campos F P V, et al, "A low lost OFDM based modulation schemes for data communication in the passband frequency", 2011 IEEE International Symposium on Power Line Communications and Its Applications, pp424-429,2011
- [5] Y. Jiang, "New companding transform for PAPR reduction in OFDM", IEEE Communications Letters, vol.14, no.4, pp282-284, 2010

- [6] E. C. Sun, R.Z. Yang, and P. B. Si, "Raised cosine-link companding scheme for peak-to-average power ratio reduction of SCFDMA signals", 2010 Global Mobile Congress, pp1-5, 2010
- [7] R. M. Mahamood, E.T. Akinlabi, Mukul Shukla, and Sisa Pityana, "Material Efficiency of Laser Metal Deposited Ti6Al4V: Effect of Laser Power", Engineering Letters, vol.21, no.1, pp18-22, 2013
- [8] K. T. Wong, B. Wang, and J. C. Chen, "OFDM PAPR reductin by switching null subcarriers and data-subcarriers", Electronic Letters, vol.47, no.1, pp62-63, 2011
- [9] A. Ghassemi, T. A. Gulliver, "A Low-Complexity PTS-Based Radix FFT Method for PAPR Reduction in OFDM Systems", IEEE Transactions on Signal Processing, vol.56, no.3, pp1161-1165, 2008
- [10] A. Ghassemi, T. Gulliver, "PAPR reduction of OFDM using PTS and error-correcting code subblocking", IEEE Trans. on Wireless Communications, vol.9, no.3, pp679-685, 2012
- [11] P. Varahram, W. F. Al-Azzo, and B. M. Ali, "A low complexity partial transmit sequence scheme by use of dummy signals for PAPR reduction in OFDM systems", IEEE Trans. on Consumer Electronics, vol.56, no.4, pp2416-2420, 2010
- [12] R.W. Bauml, R. Fischer, and J. B. Huber, "Reducing the peak-to-average power ratio of multicarrier modulation by selected mapping", Electronics Letters, vol.32, no.22, pp2056-2057, 1996
- [13] H. B. Jeon, K. H. Kim, J. S. No, and D. J. Shin, "Bit-Based SLM Schemes for PAPR Reduction in QAM Modulated OFDM Signals", IEEE Trans. on Broadcasting, vol.55, no.3, pp679-685, 2009
- [14] C. L. Wang, S. J. Ku, and C. J. Yang, "A low-complexity papr estimation scheme for ofdm signals and its application to SLM-based PAPR reduction", IEEE Journal on Selected Topics in Signal Processing, vol.4, no.3, pp637-645, 2010
- [15] E. Saberinia and A. H. Tewfik, "N-tone sigma-delta UWB-OFDM transmitter and receiver", 2003 IEEE Int. Conf. Acoustics, Speech and Signal Processing, ppIV - 129-32, 2003