Developing Experimental Learning in a Graphical Course Using Thurstone’s Law of Comparative Judgment

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Abstract—In this paper, one innovative educational experiment to help student obtain a better way to learn spatial vision in graphical course was carried out. After implementation of the improvements into a graphical engineering course, an evaluation study, through surveys, was conducted to investigate the effectiveness of this visual experiment. This empirical study provided one hundred and sixty four andalusian freshmen three types of visualization (2D static depictions, 3D computer depictions and an augmented reality environment that allows multiple participants to interact with 2D and 3D data) required to improve their skills related to spatial vision. According to results, most students showed positive attitudes toward this practice. In addition, students perceived positive impacts of this effort on their learning experience. The responses to surveys illustrated that students prefer 3D traditional learning, however they think augmented reality learning is no useful for better visual understanding of different objects.

Index Terms—Learning, spatial ability, visual experiment

I. INTRODUCTION

According to [1], along with progressive development of technology and science, computer-aided drafting (CAD) has already been a strong power to build 2D and 3D engineering graphics. The various effects within CAD can promote student’ visualization skill and deepen their understanding toward object constructions, features and performances.

Others authors regard that engineering graphics are very important due to it offers more than just teaching the technical language, it also helps develop students’ visual ability and three dimensional problem solving skills [2]-[3]. In this regard, [1] indicated that the importance of spatial visualization should be greatly emphasized due to the rapid growth of computer hardware and software technologies.

In another vein, augmented reality (AR), defined as an emerging technology with high relevance for teaching, learning and creative inquiry [4], has an important application in all engineering areas, because it allows us to interact with reality designed to verify proper use.

It is noteworthy that CAD and AR might not work for all kinds of learning. According to [5], learner characteristics or individual differences can account for different learning results in both CAD-based and AR-based learning environments. In recent years, there is more focus on the role of learner characteristics or individual differences on learning with visual representations [6]. The importance of considering individual differences in visual representations is also emphasized by [7]. The effects of learner characteristics on learning outcomes would enable instructor to adapt the nature of instruction to accommodate individual differences to improve learning outcomes [5].

Hitherto, most teaching-learning studies have attempted to apply different techniques aimed at improving student ability in all areas. However, none of them use the Thurstone theory. For this reason, the aim of this paper is to use paired comparisons to glimpse what the needs are of freshmen.

II. PRESENTATION

A. Literature Review

As [1] point out, the visual presentation of objects is expressed in a more explicit way, although pictorial drawings are occasionally used, multi-view drawings are still the main method employed in mechanical drafting for the complete description of an object. On the other hand, [8] indicate that the orthographic projection is necessary to be used for observing an object from different views, including front, side and top views, and systematically putting them on a piece of drawing paper to deliver the essential information to viewers.

As is known, in most of the time pictorial drawing can be easily understood by students without technical training [3]. According to [1], even though pictorial drawing has good
comprehension to the observers, it fails to present the complex or detailed features of an object. To overcome the defects, students can create different pictorial drawings displayed in various directions for assistance.

A person gradually learns from concrete to abstract [3]. It is be noted in connection with the foregoing that [9] made an empirical study to compare the learning effectiveness between parts-to-whole (PTW) and whole-to-parts (WTP) in teaching engineering drawing. As a result, the WTP approach proved to accelerate learning of engineering drawing and spatial visualization skills. Therefore, and according to [10], to present learners with concrete images to begin with is the best means to help them understand the features of an object.

In another vein, empirical studies have examined the use AR-based technologies for teaching and learning in engineering [11-12]. According to [4], given that mobile AR is still an emergent technology and field of study, it is not surprising that the majority of these studies is of a qualitative nature and concentrates on the elicitation of affordances and constraints of AR for teaching and learning. Hitherto, only few quantitative studies exist that rigorously measure the effect of AR on learning performance.

Most of the studies reviewed examined the effect of AR on learning spatial abilities [4]. Regarding the area of engineering, in one of the first large-scale experiments [13] investigated the efficacy of AR for training spatial abilities using 215 high school students as participants, but a between groups comparison could not find clear evidence for the advantageousness of AR as a spatial ability learning tool. In contrast to such study, [14] also studied the effect of AR on learning spatial abilities using a textbook enhanced by a desktop AR system and found more promising results, as in a pretest-posttest classroom experiment with 49 university students the AR group showed a significant gain in spatial abilities with the grades of students of the same course in the previous year (control group without AR), they found a significant statistical difference indicating that the application of AR technology in the course helped to improve students’ performance.

B. Thurstone’s Law

According to [16], Louis Leon Thurstone, in 1927, pioneered psychometrics by using Gaussian distribution to analyze paired comparisons. Thurstone’s model assumes that an option’s quality is a Gaussian random variable. This models the fact that different people may have different opinions on the quality of an option. Each option’s quality score is taken to be the mean quality of the corresponding Gaussian.

Consider the basic case of two options, where we let the Gaussian random variables $A$ and $B$ represent the quality of both option A and B as follows (1):

$$ A - N(\mu_A, \sigma_A^2), B - N(\mu_B, \sigma_B^2) $$

Their probability density functions (PDFs) are (2):

$$ p_A(a) = \frac{1}{\sigma_A} \cdot \varphi \left( \frac{a - \mu_A}{\sigma_A} \right), \quad p_B(b) = \frac{1}{\sigma_B} \cdot \varphi \left( \frac{b - \mu_B}{\sigma_B} \right) $$

where $\varphi$, $\varphi(x) = [1/(2\pi)^2] \cdot \exp(-0.5x^2)$, is the standard normal PDF (zero mean and unit variance).

Thurstone’s model says that when a person judges whether option A is better than option B, they draw a realization from A’s quality distribution and a realization from B’s quality distribution, and then chose the option with the higher quality [17]. Equivalently, they choose option A over option B if their draw from the random quality difference A-B is greater than zero, $P(A>B) = P(A-B>0)$.

Since A-B is the difference of two Gaussians, A-B is a Gaussian random variable, that is (3):

$$ A - B \sim N(\mu_{AB}, \sigma_{AB}^2) $$

$$ \mu_{AB} = \mu_A - \mu_B $$

$$ \sigma_{AB}^2 = \sigma_A^2 + \sigma_B^2 - 2 \cdot \rho_{AB} \cdot \sigma_A \cdot \sigma_B $$

where $\mu_{AB}$ is the mean quality different of A-B, $\sigma_{AB}$ is the standard deviation of the random quality difference A-B, and $\rho_{AB}$ is the correlation between A and B.

Therefore the probability of choosing option A over option B is (4):

$$ P(A > B) = P(A - B > 0) $$

$$ = \int_{0}^{\infty} \frac{1}{\sqrt{2\pi\sigma_{AB}^2}} \cdot \exp \left[ \frac{-(x - \mu_{AB})^2}{2\sigma_{AB}^2} \right] \, dx $$

$$ = \int_{-\infty}^{\mu_{AB}} \frac{1}{\sqrt{2\pi\sigma_{AB}^2}} \cdot \exp \left[ \frac{-x^2}{2\sigma_{AB}^2} \right] \, dx $$

By the symmetry of the Gaussian, (4) can be expressed (5):

$$ = \int_{-\infty}^{\mu_{AB}} \frac{1}{\sqrt{2\pi\sigma_{AB}^2}} \cdot \exp \left[ \frac{-x^2}{2\sigma_{AB}^2} \right] \, dx $$

$$ = \int_{-\infty}^{\mu_{AB}} \frac{1}{\sigma_{AB}} \cdot \Phi \left( \frac{x}{\sigma_{AB}} \right) \, dx $$

$$ = \int_{-\infty}^{\mu_{AB}/\sigma_{AB}} \Phi(t) \cdot dt = \Phi \left( \frac{\mu_{AB}}{\sigma_{AB}} \right) $$

where $\Phi(z)$ is the standard normal cumulative distribution function (CDF) (6):
By inverting (5), we can obtain the mean quality difference \(\mu_{AB}\) as (7):

\[
\mu_{AB} = \sigma_{AB} \Phi^{-1}(P(A > B))
\]

(7)

where \(\Phi^{-1}(x)\) is the inverse CDF of the standard normal [17]. The inverse CDF of the standard normal is also commonly known as the z-score or standard score since it gives the number of standard deviations that \(x\) is from the mean. Although traditionally, getting the z-score required large lookup tables, modern computers can calculate the inverse CDF function precisely [16].

According to [16], Thurstone proposed estimating \(P(A > B)\) by the empirical proportion of people preferring \(A\) over \(B\), \(C_{AB}/(C_{AB}+C_{BA})\). Assuming we can estimate the standard deviation \(\sigma_{AB}\), the estimator for the quality difference is (8):

\[
\hat{\mu}_{AB} = \sigma_{AB} \Phi^{-1} \left( \frac{C_{AB}}{C_{AB} + C_{BA}} \right)
\]

(8)

Equation (8) is known as Thurstone’s Law of Comparative Judgment.

C. Participants

One hundred and sixty four andalusian freshmen from three classes of one engineering degree (Industrial Engineering) at University of Seville (Spain) were committed to the empirical study.

This study was designed with objects displayed with different forms of isometric drawings, including 2D static and 3D animation, in addition to industrial pieces shown in AR. All participants were taught by the same instructors.

D. Display of the Views Ability Test

The topic of views ability test was "types of visualization to improve the skills of spatial vision". Four versions of display illustrated the features of objects that were used in this spatial ability test. Two versions of display were static in the forms of 2D graphics, one was exhibited by necessary and sufficient views of different industrial pieces, which were constructed by the forms of pictorial drawing (Fig. 1). The other was described as 3D computer depictions (Fig. 2) using Solid Edge ST7. The other two versions of display were presented in the form of 3D rendering graphic with Solid Edge ST7 (Fig. 3) and using the free app called Augment Reality (Fig. 4). All displays of animation were presented five times for every object. These animations were presented without verbal or written descriptions and participants could not arbitrarily control these animations [1].

According to [18], the application of 3D models might easily increase cognitive load to students with low spatial ability. Therefore, by means of slowing the animation speed, eliminating verbal or written descriptions, and increasing the frequency of the animation are beneficial to this study.

The experiment was conducted in February 2015. In this study, all objects (2D, 3D and AR) were presented as paired comparisons.

E. Analysis

After completing the visualization of all paired comparisons, all freshmen filled a simple questionnaire with ten questions. The questionnaire documented their
comprehension of orthographic views toward different versions of display. All questions were asked to determine which version of display was the participant’s favorite. Various data sources were collected to evaluate the students’ comprehensive outcomes. In order to assure the efficiency of views ability test, eleven experts’ opinions were required. All experts are professors from different Spanish universities. These experts were asked to inspect if the questionnaires were correlated to the related fields, as [1] specify.

The answers of each participant were computer-processed with adequate statistical software. Analysis of the data included comparison between different types of visualization (2D, 3D and AR), in addition to know the kind of learning that the freshmen prefer.

III. RESULTS AND DISCUSSION

Tables I and II give an overview of the test scores. In general, all results are in line with expectations. The difference between scores of the pretest and posttest could be because, at the beginning of the graphical course, freshmen had only little prior knowledge about the topics covered in this study.

The score scale of each compared pair (A vs B) were from -5 to 5 (-5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5), where 0 is equivalent to indifference between A and B. Maximum and minimum values presented in tables I and II correspond to those marked by participants.

As can be observed in tables I and II, there are significant differences between the scores of pretest and posttest. Freshmen generally positively value traditional learning, perhaps due to low use of both CAD and AR tools in high school.

Table III shows the assigned weights by participants in the pretest.

As can be appreciated in table 3, there are important differences in the evaluation of different pairs. Students positively evaluated Traditional Learning (TL), as it was expected, because in previous years the graphical course was not taught via Computer Learning (CL) or Augmented Reality Learning (ARL). It is interesting to specify the weight assigned to the pair Spatial Perception in Traditional Learning (SPTL) vs Spatial Perception in CL (SPCL), -1.688, meaning that all participants recognize the importance of TL as basis for the development of spatial perception.

With regard to ARL, and given that in the initial test had not been used, it may think, regardless of the students knew the meaning of AR (85% ignored its definition), all participants have answered based on their preferences regarding the explanation specified in class on using the tool.

**TABLE I**

<table>
<thead>
<tr>
<th></th>
<th>Min</th>
<th>Max</th>
<th>Mode</th>
<th>SD</th>
</tr>
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<tbody>
<tr>
<td>Traditional Learning</td>
<td>5</td>
<td>-5</td>
<td>3</td>
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<tr>
<td>Computer Learning</td>
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<td>-5</td>
<td>0</td>
<td>2.33</td>
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<tr>
<td>Augmented Reality Learning</td>
<td>-5</td>
<td>5</td>
<td>0</td>
<td>2.98</td>
</tr>
<tr>
<td>Spatial Perception in TL</td>
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<td>-5</td>
<td>-3</td>
<td>1.21</td>
</tr>
<tr>
<td>Spatial P. in CL</td>
<td>1</td>
<td>5</td>
<td>5</td>
<td>1.29</td>
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</table>

**TABLE II**

<table>
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<th>Min</th>
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<td>-5</td>
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<tr>
<td>Computer Learning</td>
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<td>-5</td>
<td>3</td>
<td>2.14</td>
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<td>Augmented Reality Learning</td>
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<td>5</td>
<td>4</td>
<td>2.97</td>
</tr>
<tr>
<td>Spatial Perception in TL</td>
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<td>-5</td>
<td>-2,-5</td>
<td>1.52</td>
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<tr>
<td>Spatial P. in CL</td>
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<td>5</td>
<td>3</td>
<td>1.14</td>
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</table>

**TABLE III**

<table>
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<th>CL</th>
<th>SPTL</th>
<th>SPCL</th>
<th>ARL</th>
</tr>
</thead>
<tbody>
<tr>
<td>TL</td>
<td>-0.351</td>
<td>-2.610</td>
<td>-0.974</td>
<td>-1.221</td>
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<tr>
<td>CL</td>
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<tr>
<td>SPTL</td>
<td>2.610</td>
<td>2.377</td>
<td>-1.688</td>
<td>-1.208</td>
<td></td>
</tr>
<tr>
<td>SPCL</td>
<td>0.974</td>
<td>0.857</td>
<td>1.688</td>
<td>-0.052</td>
<td></td>
</tr>
<tr>
<td>ARL</td>
<td>1.221</td>
<td>0.065</td>
<td>1.208</td>
<td>0.052</td>
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</tr>
</tbody>
</table>

Fig. 3. 3D rendering graphic with Solid Edge ST7.
Fig. 4. Augment Reality free app.
Figure 5 shows the scalar transformed values (STV) obtained from the scalar values for each item (SVI).

As was outlined, the students gave more importance to TL, because for them it is essential vehicle for the development of spatial perception (Fig. 5).

In order to see the evolution followed by all participants, an external evaluation was conducted in mid-February 2015. External evaluators were in classes observing the work of the students and after, they filled the same survey that those, with the difference that marked refer to how external evaluators perceived the development of freshmen via comparison pairs. The assigned weights by external evaluators and the STV are shown in table IV and Fig. 6 respectively.

External evaluators specified that ARL has no benefit in comparison with CL.

After making the improvements suggested by external evaluators, in late February 2015 the latest survey was performed, whose results are shown in table V and figure 7.

As can be appreciated in Fig. 7, students think for a proper understanding of the graphical course is required a theoretical basis based on TL and use of software that improves the overview, in 3D, of the represented object. For this reason, the STV of SPCL are null in both pretest (Fig. 5) and posttest (Fig. 7). In this final test all participants think ARL has not an important role to obtain a spatial understanding of the object. Likewise ARL neither favors the development of spatial ability of students.

According to external evaluation, students better understand teaching-learning processes based on TL. However, although the use of new technologies applied to engineering degrees is booming since 2006 [4], students still have a great disconnect between the relationship of the object in 2D and its three-dimensional spatial projection.

### IV. CONCLUSIONS

Recent advances in mobile technologies (tablets and iPods with cameras, internet access [19-20] and GPS) may be a great opportunity for development of new strategies to enable the appropriate development of spatial vision skills in graphical courses. However, it is necessary to consider the attitude of participants, as it is along with their particular characteristics of prior knowledge and effort which allows adequate results.

In this study, the evolution of spatial vision skills depended on the atmosphere created by the professor in class, with...
appropriate exercises, since in University of Seville each practice group has between 24 and 48 students, very far from the 5-10 participants per group with which [7] conducted their study, reason why collaborative strategies should have better results in those universities which, such as ours has still a high rate of students per professor.

As for assessing the freshmen’ spatial perception skills, 3D animations can increase the effects of good performances. Thus, it’ll probably become a more accurate way to evaluate the participants’ orthographic views’ ability.

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REFERENCES


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