Real-Time Nonlinear Optimal Control of a Hydraulic Actuator

F. Liccardo, S. Strano and M. Terzo

Abstract— This paper presents a nonlinear control for a hydraulic actuator with significant nonlinearities. These are the key factors causing delay and error in the hydraulic actuation response and highly limit the performances of the classical linear control. Hence, a nonlinear control design based on the mathematical model of the hydraulic actuator is employed.

The proposed approach consists of a nonlinear feedback control based on the state-dependent Riccati equation (SDRE). The control performance is demonstrated by both simulations and real-time experiments.

The experimental results validate the proposed approach and highlight a good accordance with simulations.

Index Terms— Hydraulic actuator, optimal control, SDRE, Riccati equation, nonlinear, tracking, real-time.

I. INTRODUCTION

HORAULIC actuators employ hydraulic pressure to drive an output member. These are used where high speed and large forces are required. The fluid used in hydraulic actuator is highly incompressible so that pressure applied can be transmitted instantaneously to the attached member.

Hydraulic components, because of their high speed and pressure capabilities, can provide high power output with small weight and size in comparison to electric system components. Hydraulic actuators can be found in transportations, industrial machineries, seismic applications [1], and earth moving equipments. However, the dynamics of hydraulic systems are highly nonlinear [2] due to the pressure-flow rate relationship, the dead band of the control valve and the frictions. These nonlinearities highly limit the performance achieved by the classical linear controller.

In the past, much of the work in the control of hydraulic systems has used linear model [3] or local linearization of the nonlinear dynamics about the nominal operating point [4]. Suitable adaptive approaches are employed when there is no knowledge of the parameter values [5], [6], [7]. In order to take system uncertainties into account, robust approaches can be adopted [8], [9]. In [10], a sliding mode

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control applied to an asymmetric single-rod cylinder was presented.

In this paper a SDRE-based control for a hydraulic actuator is proposed and applied to a hydraulic cylinder of a seismic test bench. The basic idea of the SDRE technique is to capture the nonlinearities by bringing the nonlinear system to a linear structure having state-dependent coefficient (SDC) matrices, and minimizing a nonlinear performance index having a quadratic-like structure [11]. The suboptimal control action can be obtained solving online an algebraic Riccati equation (ARE) using the SDC matrices [12].

This paper continues the work done in [13] and [14] and shows experimental results in order to validate the proposed nonlinear approach.

The rest of the paper is organized as follows: a description of the proposed control is given in Section II. In Section III the nonlinear model of the hydraulic actuator is derived and in Section IV the control has been particularized the specific system. Simulation results are reported in Section V and in Section VI the main experimental results are presented.

II. SDRE FORMULATION

Consider a nonlinear observable systems represented in general form by equations

$$\dot{x} = f(x, u) \tag{1}$$

where $x \in \mathcal{Q}^n$ and $u \in \mathcal{Q}^m$ are the state and the control respectively.

Assume that the origin is an equilibrium point and suppose that the dynamic model of the system can be placed in the SDC form

$$\dot{x} = A(x)x + B(x)u . \tag{2}$$

Consider the autonomous, infinite-horizon, nonlinear regulator problem of minimizing the performance index

$$J = \frac{1}{2} \int_0^\infty \left\{ x^T Q x + u^T R u \right\} dt$$
(3)

with respect to the state x and the control u, subject to the nonlinear differential constraints (2); where $Q \ge 0$ and R > 0 are symmetric weighting matrices. The SDRE control method provides an approximate nonlinear feedback solution of the above problem. The feedback gain equation

is given as

$$K(x) = -R^{-1}B^{\mathrm{T}}(x)P(x)$$
(4)

where P(x) is the symmetric, positive-definite solution of the SDRE of the form

$$A^{T}(x)P(x) + P(x)A(x) + Q -P(x)B(x)R^{-1}B^{T}(x)P(x) = 0$$
(5)

The SDRE controller can be implemented as a servomechanism, similar to the that of a linear quadratic regulator [15]. Given a desired state trajectory x_d , the SDRE servo control action is then given by

$$u_{SD} = -R^{-1}B^{\mathrm{T}}(x)P(x)(x-x_d).$$
(6)

III. DYNAMICAL MODEL OF THE HYDRAULIC ACTUATION SYSTEM

In order to describe the behaviour of the system, a set of differential equations is derived in the following. The hydraulic actuator under consideration consists of a doubleended hydraulic cylinder driven by a four-way spool valve. The hydraulic cylinder is coupled to a mass that moves on linear guides (Fig. 1).

For the derivation of the mathematical model, the following hypothesis have been adopted: a) fluid properties not depending on the temperature; b) equal piston areas; c) equal oil volume for each side (with the barrel in a central position); d) negligible internal and external fluid leakages; e) tank pressure equal to zero. The dynamics of the movable mass displacement (y) is governed by

$$m\ddot{y} + \sigma \dot{y} + F_f(\dot{y}) = A_p P_L , \qquad (7)$$

where *m* is the mass of the load, σ is the viscous friction coefficient, F_f is the friction force, A_p is the piston area, $P_L = P_A - P_B$ is the load pressure, P_A and P_B are the pressures inside the two chambers of the cylinder.

The friction force is represented by the following equation

$$F_{f}(\dot{y}) = \begin{cases} F_{c} \operatorname{sgn}(\dot{y}) + \mu mg \operatorname{sgn}(\dot{y}) & \dot{y} \neq 0 \\ Z & |Z| \leq F_{c0} + \mu_{0} mg & \dot{y} = 0 \end{cases}$$
(8)

where F_c is the Coulomb friction force in the hydraulic actuator (assumed equal to its static value F_{c0}), μ is the Coulombian friction coefficient of the linear guides (assumed equal to its static value μ_0), g is the gravitational acceleration and Z is the net tangential force that acts on the actuator when it is not moving [16].

The load pressure dynamics [2] is given by

$$\frac{V_0}{2\beta}\dot{P}_L = -A_p\dot{y} + Q_L \tag{9}$$

where V_0 is the volume of each chamber for the centered position of the piston, $Q_L = (Q_A + Q_B)/2$ is the load flow and β is the effective Bulk modulus.

An overlapped four-way valve is considered: typically, this kind of valve is characterized by the lands of the spool greater than the annular parts of the valve body. Consequently, the flow rate is zero (*dead band*) when the spool is in the neighbourhood of its central position

The load flow depends on the supply pressure, the load pressure and the valve spool position in accordance with the following

$$Q_L = \Psi(v_e) v_e \sqrt{P_s - |P_L|} \tag{10}$$

where v_e is the displacement signal of the spool value and $\Psi(v_e)$ is a variable gain functional to describe the value dead band.

The analytical expression of $\Psi(v_e)$ can be assumed as

$$\Psi(v_e) = \begin{cases} k_{qp} \left(1 - \frac{v_{ep}}{v_e} \right) & v_e > v_{ep} \\ 0 & v_{en} \le v_e \le v_{ep} \\ k_{qn} \left(1 - \frac{v_{en}}{v_e} \right) & v_e < v_{en} \end{cases}$$

$$(11)$$

where the pairs (v_{en}, v_{ep}) and (k_{qn}, k_{qp}) are the dead band widths and the gains for the positive and negative spool displacement, respectively. The dead band nonlinearity is among the key factors causing delay and error in the hydraulic actuation response [17], [18].

The proportional valve dynamics can be well represented by a second order differential equation [19]

$$\frac{\ddot{v}_e}{\omega_{nv}^2} + \frac{2\xi_v}{\omega_{nv}}\dot{v}_e + v_e = k_e u + v_{e0}$$
(12)

where parameters ω_{nv} and ξ_v are the natural frequency and the damping ratio of the valve respectively, v_{e0} is the spool position bias, k_e is the input gain and u is the valve command.



Fig. 1. Schematic diagram of the hydraulic actuation system.

Finally, the equations governing the dynamics of the whole system (movable mass + hydraulic system) are

$$\begin{cases}
m\ddot{y} + \sigma\dot{y} + F_{f}(\dot{y}) = A_{p}P_{L} \\
\frac{V_{0}}{2\beta}\dot{P}_{L} = -A_{p}\dot{y} + Q_{L} \\
Q_{L} = \Psi(v_{e})v_{e}\sqrt{P_{s} - |P_{L}|} \\
\ddot{v}_{e} = -\omega_{m}^{2}v_{e} - 2\xi_{v}\omega_{mv}\dot{v}_{e} + \omega_{mv}^{2}(k_{e}u + v_{e0})
\end{cases}$$
(13)

The developed fifth order model fully describes the nonlinear dynamical behavior of the hydraulic actuation system and takes the nonlinear friction forces and the nonlinear flow rate distribution into account.

The system (13) can be written in the following form

$$\begin{cases} \ddot{y} = -\frac{\sigma}{m} \dot{y} - \frac{F_f(\dot{y})}{mv_e} v_e + \frac{A_p P_L}{m} \\ \dot{P}_L = -\frac{2\beta A_p}{V_0} \dot{y} + \frac{2\beta \Psi(v_e) \sqrt{P_s - |P_L|}}{V_0} v_e \\ \ddot{v}_e = -2\xi_v \omega_{nv} \dot{v}_e - \left(1 - \frac{v_{e0}}{v_e}\right) \omega_{nv}^2 v_e + \omega_{nv}^2 k_e u \end{cases}$$
(14)

The system (14), represented in the state space form, is nonlinear in the state, autonomous and characterized by a fully known state by means of measurements.

It is possible to note in the first and the third equation of (14) a division by the variable v_e , as well as happens in (11). In order to prevent divisions by zero, has been introduced a functional variable $\tilde{v}_e = v_e + \varepsilon$, where ε is given by:

$$\varepsilon = \begin{cases} \Delta v_e & v_e = 0\\ 0 & \text{otherwise} \end{cases}$$
(15)

where the value of Δv_e is chosen less than the minimum acceptable measurement error of the valve spool position v_e .

Substituting the variable \tilde{v}_e into the fractions of (14) and (11) follows:

$$\begin{cases} \ddot{y} = -\frac{\sigma}{m} \dot{y} - \frac{F_f(\dot{y})}{m \tilde{v}_e} v_e + \frac{A_p P_L}{m} \\ \dot{P}_L = -\frac{2\beta A_p}{V_0} \dot{y} + \frac{2\beta \Psi(\tilde{v}_e) \sqrt{P_s - |P_L|}}{V_0} v_e \\ \ddot{v}_e = -2\xi_v \omega_{nv} \dot{v}_e - \left(1 - \frac{v_{e0}}{\tilde{v}_e}\right) \omega_{nv}^2 v_e + \omega_{nv}^2 k_e u \end{cases}$$
(16)

IV. PARAMETERIZATION OF THE SDRE CONTROL

This section explains the design of the SDRE controller. The SDC parameterization has been performed using the highly nonlinear equations (16).

The matrices in (2) have been chosen as follows:

$$A(x) = \begin{bmatrix} -\frac{\sigma}{m} & 0 & \frac{A_p}{m} & 0 & -\frac{F_f(\dot{y})}{m\tilde{v}_e} \\ 1 & 0 & 0 & 0 & 0 \\ -\frac{2\beta A_p}{V_0} & 0 & 0 & 0 & \frac{2\beta \Psi(\tilde{v}_e)\sqrt{P_s - |P_L|}}{V_0} \\ 0 & 0 & 0 & -2\xi_v\omega_{nv} & -\left(1 - \frac{v_{e0}}{\tilde{v}_e}\right)\omega_{nv}^2 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}$$
(17)

where the state vector is $x = \begin{bmatrix} \dot{y} & y & P_L & \dot{v}_e & v_e \end{bmatrix}^{\mathrm{T}}$.

The matrix B does not depend on the state and is given by:

$$B = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ \omega_{nv}^{2} k_{e} \\ 0 \end{bmatrix}.$$
 (18)

For the specific problem, without loss of generality, the goal of the tracking control is that the movable mass follows a desired displacement $y_d(t)$; therefore, the weighting matrices in (3) become: $Q = diag(0, q_{SD}, 0, 0, 0)$ and $R = r_{SD}$, where q_{SD} and r_{SD} are two weighting coefficients.

V. SIMULATION RESULTS

In this section some simulation results, concerning the application of the proposed controller to a particular hydraulic actuation system presented in Section VI, are reported. The physical parameter values of the hydraulic actuator are:

$$m = 441 \text{ kg}, \ \sigma = 23555 \ \frac{\text{N} \cdot \text{s}}{\text{m}}, \ F_C = F_{C0} = 950 \text{ N},$$

 $\mu = \mu_0 = 0.01, \ N = 4326 \text{ N}, \ A_p = 0.01 \text{ m}^2,$

$$V_{0} = 0.004 \text{ m}^{3}, \ \beta = 1e9 \text{ Pa}, \ k_{qp} = 6.15e - 7 \frac{\text{m}^{3}}{\text{s} \cdot \text{V} \cdot \text{Pa}^{\frac{1}{2}}},$$
$$k_{qn} = 5.86e - 7 \frac{\text{m}^{3}}{\text{s} \cdot \text{V} \cdot \text{Pa}^{\frac{1}{2}}}, \ v_{ep} = 0.43 \text{ V}, \ v_{en} = -0.21 \text{ V},$$
$$v_{e0} = 0.01 \text{ V}, \ k_{e} = 0.49, \ \omega_{nv} = 152.30, \ P_{S} = 6e6 \text{ Pa}.$$

These parameters have been obtained with a parameter identification technique [13].

The controller is used for tracking sinusoidal motion trajectory characterized by an amplitude of 0.04 m and a frequency of 1 Hz.

The simulation results reported in Fig. 2 consist of comparisons between the target and the effective movable mass displacement, the tracking error $(y - y_d)$ and the control action.



Fig. 2. Simulation results of the nonlinear SDRE-based control.

The maximum value of the tracking error is about 0.008 m. The difference between the peak to peak amplitude of the effective displacement and the target one is about 0.001 m, and the actuation system phase lag is of 0.03 s.

To verify the prediction capacity of simulation, the results reported in Fig. 2 will be compared with the experimental ones.

VI. REAL-TIME EXPERIMENTS

In order to test the effectiveness of the proposed nonlinear tracking controller, experimental studies are conducted on the hydraulic actuation system of the test rig shown in Fig. 3 [20], [21], [22].

A. The experimental test rig

The experimental test rig is a machine utilized to perform shear tests on seismic isolators [23], [24], [25]. The actuation system consists of a double-ended hydraulic actuator placed between a fixed base and a sliding table (1.8 m x 1.59 m). The hydraulic actuator is constituted by a mobile barrel, integral with the sliding table (A), and two piston rods linked to the fixed base (B) (Fig. 3). The isolator under test (C) is located between the sliding table and a slide that can move vertically with respect to the horizontal reaction structure (D).

A hydraulic jack (E) is positioned between the vertical reaction structure (F) and the slide in order to make the isolator under test vertically loaded.

The supply circuit of the hydraulic actuator is mainly constituted by an axial piston pump, powered by a 75 kW AC electric motor, a pressure relief valve and a four way-three position proportional valve [26]. The pump is characterized by a variable displacement and it is able to generate a maximum pressure of 210 bar and a maximum flow rate equal to 313 l/min.



Fig. 3. Experimental test rig.

The maximum horizontal force is 190 kN, the maximum speed is 2.2 m/s and the maximum stroke is 0.4 m (\pm 0.2 m).

The removal of the reaction structures allows the testing machine to be used as a shaking table [27].

The full-state feedback has been obtained with the following measurements:

- table position by means of magnetostrictive position sensor (FS = 0.4 m - estimated uncertainty = ± 1.2e-4 m);
- pressure in the two chambers of the hydraulic cylinder by means of strain gauge sensor (FS = 400 bar estimated uncertainty = ± 1 bar);
- valve spool position by means of built-in LVDT sensor;

A dSPACE DS1103 controller board, equipped with a 16-bit A/D and D/A converter, has been used for the realtime experiments. All experiments have been conducted with a sample frequency of 1 kHz. To attenuate the influence of the noise, all measured signals are processed through a low-pass filter. The supplied pressure has been fixed to 6e6 Pa.

B. Experimental Results

The experiments on the seismic isolator testing machine have been conducted without the isolator to be characterize. Hence, the hydraulic actuation system has been utilized only for the sliding table positioning.

For sake of comparison, the experimental validation of the proposed control has been obtained with the same target displacement imposed to the movable mass in the simulations.

The problem of computing the SDRE feedback gains

reduces to solving (5). The proposed approach is based on finding the eigenvalues of the associated Hamiltonian matrix [28], [29], defined as

$$H(x) = \begin{bmatrix} A(x) & -B(x)R^{-1}B^{T}(x) \\ -Q & -A^{T}(x) \end{bmatrix}.$$
 (19)

The SDRE-based feedback gains have been obtained with a pole placement algorithm in terms of the stable eigenvalues of H(x).

The SDRE feedback action has been implemented as a Ccode function downloaded to the controller board and implemented in real-time.

In Fig. 4 are reported the experimental results in terms of the target and the experimental effective table displacement, the tracking error and the control action.



Fig. 4. Experimental results of the nonlinear SDRE-based control.

Analyzing the experimental results, it is possible to assert that the maximum amplitude error is equal to 3e-5 m and the actuator phase lag is equal to 0.035 s. Concerning the tracking error, its maximum value is equal to 0.009 m.

The experimental results agrees with the results predicted in simulation environment.

It has been experimentally demonstrated that the proposed nonlinear controller can achieve very good performance in terms of tracking control and stability.

VII. CONCLUSION

In this paper has been proposed an optimal control using the SDRE for a hydraulic actuator. A fifth order dynamic model of the system has been derived taking into account the typical nonlinearities of the hydraulic actuators. The parameterization of the SDRE feedback control has been obtained directly from the fifth order model. The real-time implementation of the SDRE nonlinear optimal problem has been performed with a pole placement algorithm in terms of the stable eigenvalues of the Hamiltonian matrix.

Experiments have been conducted on the hydraulic actuation system equipped on a seismic isolator test rig. The

experimental results validate the proposed approach and highlight a good accordance with simulation results.

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